

# DEFINING THE LAW FOR THE DISTRIBUTION OF AVERAGE MONTHLY EXPENDITURES IN THE ZARAFSHAN AND SURKHANDARYA RIVERS

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## Abstract

In analytical groups, quantitative features are mainly used. They are also applied when constructing distribution rows. When grouping, on quantitative characteristics, questions arise about the number of groups and value - the width of the interval. These indicators are interconnected, the more groups are cut, the less the interval, and vice versa.

**Keywords:** water in the reservoir, full elections, incomplete elections, conditions of regularity  
Kramer-RAO, Fisher's information.

## ОПРЕДЕЛЕНИЕ ЗАКОНА РАСПРЕДЕЛЕНИЯ СРЕДНЕМЕСЯЧНЫХ РАСХОДОВ В РЕКЕ ЗАРАФШАН И СУРХАНДАРЬИ

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## Аннотация

В аналитических группировках в основном применяются количественные признаки. Они применяются также при построении рядов распределения. При группировке по количественным признакам возникают вопросы о числе групп и величине – ширине интервала. Эти показатели между собой связаны, чем больше будет нарезано групп, тем меньше будет интервал, и наоборот.

**Ключевые слова:** воды в водохранилище, полные выборы, неполные выборы, условия регулярности Крамера-Рао, информация Фишера.

## Introduction

In analytical groupings, quantitative features are mainly used. They are also used when constructing distribution series. When grouping by quantitative features, questions arise about the number of groups and the size - the width of the interval. These indicators are interconnected, the more groups are cut, the smaller the interval will be, and vice versa.

When solving the problem, it is necessary to take into account the range of variation, the variation series, which is the difference between the maximum and minimum values of the feature.



The relationship between the number of groups  $n$  and the number of units in a population  $N$  is expressed in the formula of the American scientist Sturges  $n = 1 + 3.322 \text{Lg}N$ . This dependence can serve as a guide when determining the number of groups in the event that the distribution of units of the population by a given characteristic approaches a normal distribution.

The interval size in this case is determined by dividing the range of variation by the number of groups:

$$h_0 = \frac{Q_{max} - Q_{min}}{1 + 3,222\text{Lg}N}$$

Note where –  $h_0$  is the interval width

$Q_{max}$  – water flow of the Tupalang River for the period 1928 – 1962 · m<sup>3</sup> / sec

$Q_{min}$  – min water flow m<sup>3</sup> / sec

According to our grouping: 1- interval, % of hit – 41.6, i.e. 180 cases; 2- interval, 23.6% – 102 cases; 3- interval, 13% - 56 cases; 4- interval, 10.6% - 46 cases; 5- interval, 7.3% - 32 cases; 6- interval, 1.3% - 6 cases; 7- interval, 0.2% - 1 case.

The Zarafshan River near the Dupula Bridge hydropost Twelve groups were formed along the Zarafshan River. 1 – interval, % - 50.57; 2 – interval, 17.11; 3 – interval, 7.5%; 4 – interval, 2.5%; 5 – interval, 3.26; 6 – interval, 5.76%; 7 – interval, 5.38%; 8 – interval 4.23%; 9 – interval, 1.53%; 10 – interval, 1.34%; 11 – interval, 0.57%; 12 – interval, 0.19%.

The above example shows that the water consumption of the Zarafshan and Surkhandarya rivers obeys an exponential law.

Exponential distribution. One of the distributions most frequently encountered in reliability theory is the one-parameter exponential distribution, defined by the probability density function:

$$f(x; \theta) = \begin{cases} \frac{1}{\theta} e^{-\frac{x}{\theta}}, & x \geq 0 \\ 0, & x < 0 \end{cases}$$

$$F(x) = \begin{cases} \frac{1}{\theta}, \int_0^x e^{-x/\theta} dx = 1 - e^{-\frac{x}{\theta}}, & x \geq 0 \\ 0, & x < 0 \end{cases}$$

Reliability functions

$$R(t) = \begin{cases} \int_t^{\infty} e^{-x/\theta} dx = e^{-t/\theta}, & t \geq 0, \\ 1, & t < 0, \end{cases}$$

$$h(t) = \frac{1}{\theta} \frac{e^{-t/\theta}}{e^{-t/\theta}} = \frac{1}{\theta}$$



Properties

Properties of the Exponential Distribution

Characteristic function

$$M_x(t) = (1 - \theta i)^{-1}, t < 1/\theta$$

Average

$$\mu = \theta$$

Dispersion

$$\sigma^2 = \theta^2$$

The third central moment

$$\mu_3 = 2\theta^3$$

The fourth central moment

$$\mu_4 = 9\theta^4$$

Asymmetry coefficient

$$\eta = 1$$

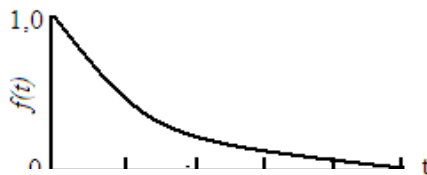
Coefficient of kurtosis

$$\alpha_3 = 2$$

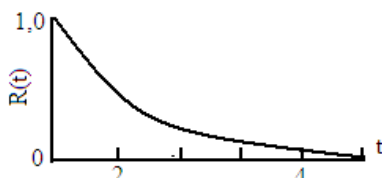
Characteristic function

$$\alpha_4 = 9$$

$$f(t; \theta) = \begin{cases} \frac{1}{\theta} e^{-t/\theta}, & t \geq 0, \\ 0, & t < 0 \end{cases}$$



$$R(t) = e^{-t/\theta}, t \geq 0$$



$$h(t) = \frac{1}{\theta}$$

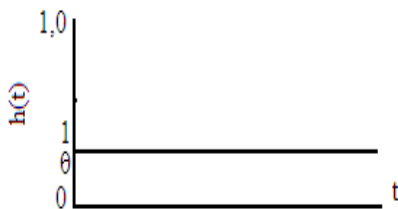


Figure 1. Functions  $f(t)$ ,  $R(t)$  and  $h(t)$  for the exponential distribution

Notes

1 The exponential distribution is a special case of both the gamma distribution and the Weibull distribution .

2 This distribution is characterized by a constant water flow rate  $1/\theta$ , which also serves as a parameter of the distribution. A constant water flow rate means that the probability of water flow does not depend on how long it has been flowing before the moment in time under consideration.



Table 1. - Histogram of the Surkhandarya river basin at the Shurchi village hydropost 1931-1962.

No.	range , m3 / sec	Number of months falling within the interval ( pcs )	% hit	Sum	
1	11.7-28.9		28.9	89	
2	29-97.72		47.7	147	
3	97.73-132.13		6.1	19	
4	132.14-166.54		4.8	15	
5	166.55-200.95		4.8	15	
6	200.96-235.36		3.57	11	
7	235.37-269.77		2.27	7	
8	269.78-304.18		13	4	
9	304.19-338.59		13	1	
				111.46	308

Determination of the step interval at the Shurchi hydropost

$$h_0 = \frac{Q_{max} - Q_{min}}{3.303 + inN} = \frac{221 - 5,71}{3.303 + in372} = 36.54$$

$$h_1 = Q_{min} + h_0 = 5.71 + 18.27 = 24.16$$

$$h_2 = h_1 + h_0 = 24.16 + 36.54 = 60.70$$

$$h_3 = h_1 + h_0 = 60.70 + 36.54 = 97.24$$

$$h_4 = h_1 + h_0 = 97.24 + 36.54 = 133.78$$

$$h_5 = h_1 + h_0 = 133.78 + 36.54 = 170.32$$

$$h_6 = h_1 + h_0 = 170.32 + 36.54 = 206.86$$

$$h_7 = h_1 + h_0 = 206.86 + 36.54 = 243.4$$

Table 2 - Histogram of the Surkhandarya river basin , Tupalang river right in Tupalangskey reservoir .

No.	Interval consumption m3 / sec	Number of months falling within the interval ( pcs )	% hit	sum
1	5.71-24.16		41.6	180
2	24.17-60.70		23.6	102
3	60.71-97.24		13	56
4	97.25-133.78		10.1	46
5	133.79-170.32		7.3	32
6	170.33-206.86		1.3	6
7	206.87-243.4		0.2	1
			97.6%	433

Determination of the width of the interval of the river. Surkhandarya village Zhdanova

$$h_0 = \frac{Q_{max} - Q_{min}}{3.303 + inN} = \frac{329 - 117}{3.303 + in372} = \frac{317.3}{9.22} = 34.41$$

$$h_1 = Q_{min} + h_0 = 11.7 + 34.41 = 28.9$$

$$h_2 = h_1 + h_0 = 28.9 + 34.41 = 63.31$$

$$h_3 = h_1 + h_0 = 63.31 + 34.41 = 97.72$$

$$h_4 = h_1 + h_0 = 97.72 + 34.41 = 132.13$$

$$h_5 = h_1 + h_0 = 132.13 + 34.41 = 166.54$$



$$h_6 = h_1 + h_0 = 166.54 + 34.41 = 200.95$$

$$h_7 = h_1 + h_0 = 200.95 + 34.41 = 235.36$$

$$h_8 = h_1 + h_0 = 235.36 + 34.41 = 269.77$$

$$h_9 = h_1 + h_0 = 269.77 + 34.41 = 304.18$$

$$h_{10} = h_1 + h_0 = 304.18 + 34.41 = 338.59$$

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